## STRATA2003

# Little Known PVS Interfaces

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- Software is organic
- It should be extensible through scripts and programs
- It should be embeddable within other software
- PVS has these capabilities, but they are not widely advertised
- This talk is an attempt to partly remedy this gap

# PVS History

- Started in 1990 as an attempt to fill the gap between proof checkers and theorem provers based on EHDM experience

- Designed to exploit the synergy between an expressive specification language and automation through powerful decision procedures

- Internal prototypes working in 1992
- First release at FME'93
- PVS 2 released in 1995 after significant design and code revision
- PVS 3 released in July 2002
- Current version 3.1 released in February 2003

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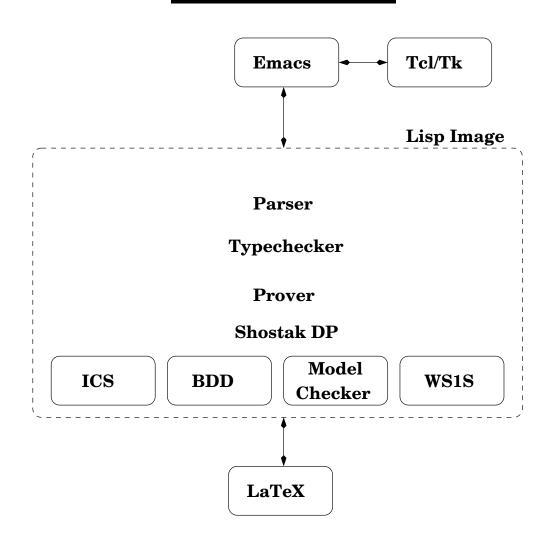
Significant Milestones

- 1993: BDD-based proposition simplification
- 1994: model checker
- 1996: new decision procedure prototype
- 1998: Mona, ground evaluator
- 2001: Theory interpretations, coinduction, cotuples
- 2002: ICS integration

How is PVS used?

- Directly as a proof checker by SRI, NASA, many others
- To teach courses at Stanford, many others
- As a back-end theorem prover by PAMELA, PVS/Maple, LOOP, InVeSt, TLPVS
- As a semantic framework through shallow embeddings: PC/DC, Ag, TAME
- Maple inteface ships formulas to PVS to be typechecked and proved
- Zeus runs on windows connected to PVS with RPC, originally interfaced to Z/Eves

# PVS Architecture



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Summary of PVS Interfaces

- The front end: User Interfaces
- The inside:
  - $\circ$  strategies
  - data structures
  - $\circ$  functions
  - embeddings
- The back end: Inference Engines, Decision procedures

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The PVS Front End

- The front end consists of Emacs, Tcl/Tk, LATEX, and Lisp functions
- In usual startup the pvs shell script runs Emacs, which loads PVS Emacs files, and starts the Lisp process
- Many systems provide their own interface, and want to use PVS as a black box, with or without Emacs
- Maple, Zeus run PVS without Emacs

PVS without Emacs

- Invoke using pvs -raw
- Reads Lisp forms from stdin
- Writes various forms to stdout, stderr
- Need to recognize the prompt, asynchronous output, and result
- None of this is documented, though it is possible to reverse-engineer from the PVS Emacs sources



- Strategies are interpreted by the PVS prover
- They employ a Lisp-like language, but they are not Lisp
- Some strategies particularly if and let do lisp evaluation for select components
- The manuals do not give adequate information about the available lisp functions and structures

The Strategy Language

There are primitive rules, defined rules, and strategies Examples of primitive rules:

- **flatten** for disjunctive simplification
- **split** for conjunctive splitting
- **skolem** for eliminating universal-strength quantifiers
- inst for instantiating existential-strength quantifiers
- **auto-rewrite** for installing rewrite rules for use during simplification
- simplify for simplification using rewriting and ground
   decision procedures



- defstep: creates a defined rule and a strategy (defstep\$)
- **defstrat**: creates a strategy only
- defhelper: like defstep, but not intended for a user command
- These all create strategies with Lisp-like arguments (&optional, &rest)
- Note that & optional and & rest also play the role of & key

Strategy Components

- calls to other rules and strategies
- quote identity strategy
- try for subgoaling and backtracking
- if for conditions
- let binds local variables to Lisp values
- recursion

A Simple PVS Strategy: smash

- smash is similar to grind, but less powerful
- It repeatedly tries bddsimp, assert, and lift-if
- Stops when all three strategies have no effect on remaining subgoals
- Note that it never (directly) evaluates Lisp expressions

decompose-equality is used to create component equalities from tuple, record, function, cotuple, and datatypes

```
{-1} r1 = (# x := 0, y := 1 #)
   |------
Rule? (decompose-equality)
Applying decompose-equality,
this simplifies to:
ff :
   {-1} r1'x = 0
   {-2} r1'y = 1
   |------
```

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- This strategy uses let and if, so directly evaluates Lisp expressions
- It uses let to build strategies, which are then invoked
- The global variable \*ps\* is bound to the current proofstate
- An appropriate equality is found in the current-goal sequent using select-seq and find-if

```
(defstep decompose-equality (&optional (fnum *) (hide? t))
  (let ((sforms (select-seq (s-forms (current-goal *ps*)))
                             (if (\text{memq fnum }'(* + -)) fnum
                                 (list fnum))))
        (fm (find-if
                #'(lambda (sf)
                     (or (decomposable-equality? (formula sf))
                         (and (negation? (formula sf))
                              (decomposable-equality?
                               (args1 (formula sf)))))
              sforms))
        (ffm (when fm (formula fm)))
        (equality? (when fm
                      (or (equation? ffm)
                          (and (negation? ffm)
                               (disequation? (args1 ffm))))))
```

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The component-equalities creates equations depending on the common type of the lhs and rhs - record, tuple, cotuple, function, or datatype

Note that if here is Lisp, not a strategy

The strategy is now built from the values of the let variables

\*new-fmla-nums\* set to fnums of new and changed formulas

```
(if fmla
  (if equality?
      (apply-extensionality fnum :hide? hide)
      (branch (case comp-equalities)
            ((then (let ((fnums *new-fmla-nums*))
                (simplify fnums))
                (if (null *new-fmla-nums*)
                  (let ((msg (format nil
                         "Generated equation ~
                         simplifies to true:"% ~a"
                         comp-equalities)))
                (then (skip-msg msg) (fail)))
```

```
(let ((fnums (find-all-sformnums
                                      (s-forms (current-goal *ps*))
                                      '* #'(lambda (x) (eq x ffm))))
                              (fnum (if fnums (car fnums) nil)))
                          (if (and hide? fnum
                                   (/= (length (s-forms
                                                 (current-goal *ps*)))
                                       fnum-count))
                              (delete fnum)
                              (skip))))
                   (flatten))
             (then (flatten) (replace*)
                   (grind :defs nil :if-match nil)))))
(skip-msg "Couldn't find a suitable equation")))
```

PVS Abstract Syntax

- PVS abstract syntax is represented in CLOS
- Every class in PVS has a corresponding recognizer with "?" suffix
- These satisfy the class hierarchy (name-expr? x) implies (expr? x)
- Hierarchy is used to hide "syntactic sugar":
  - $\circ$  +(x, 1) is of class application,
  - $\circ x + 1$  is of class infix-application,
  - o infix-application is a subclass of application
- Only the prettyprinter needs infix-application methods.



In defining strategies (among other things), it is common to create new expressions from existing ones.

PVS provides several options for this

- Use make-instance to create instances including slots unreadable and error prone
- Create a string, parse and typecheck it slow and possibly ambiguous
- Use mk- functions still need typechecking
- Use make- functions does typechecking
- Use make!- functions no typechecking, and no TCCs

Note that for typechecking, \*current-context\* must be set

Manipulating PVS Syntax: Examples

- (pc-typecheck (pc-parse "x + 1" 'expr))
- (mk-application (mk-name-expr '+) (mk-name-expr 'x) (mk-number-expr 1))
- (make-application plus (mk-name-expr 'x) (mk-number-expr 1)) where plus is set to the typechecked + operator
- (make!-application plus xxx one) where xxx and one are typechecked



- Syntactic equality is not often used because of overloading and type inferencing
- The test for equality is tc-eq, which compares two typechecked terms
  - Deals with  $\alpha$ -equivalence
  - Ignores syntactic sugar (e.g., infix vs prefix)
  - Handles overloaded names properly
- There are also useful tests for types: compatible?, subtype-of?

Substitution Functions

There are several functions for substitution:

- copy copies given term, with specific slot value settings
- lcopy makes copies only when slot values differ
- **substit** substitutes expressions for free variables
- subst-mod-params substitutes actual parameters for free parameters; also does mappings
- gensubst generic substitution



- mapobject applies a given function recursively to abstract syntax
- simplify-expr given a boolean expression, a theory, and a strategy, returns subgoals left after proof attempt
- simplify-expression given an expression (of any type), a theory, and a strategy, returns a simplified expression of the same type

Embeddings

AC/DC provided a an alternative grammar, modified from the PVS input to Ergo

- parser, unparser automatically generated
- needed to map to existing PVS classes
- generally worked, though could sometimes slip into PVS
- Ergo is not easy to work with

Ag uses a shallow embedding, with modified prettyprinter to present formulas naturally

This should be made part of the API

Adding an Inference Procedure

- PVS currently has no support for adding derived rules requires some form of reflection
- The addrule macro may be used to add new primitive rules
- Must be done carefully, potentially unsound
- Currently not documented, requires understanding of prover architecture

A Simple Inference Procedure: case

```
(addrule 'case nil (&rest formulas)
 (case-rule-fun formulas)
 "Splits according to the truth or falsity of the formulas in
 FORMULAS.
(CASE a b c) on a sequent A |- B generates subgoals:
 a, b, c, A |- B;
 a, b, c, A |- B;
 a, b, A |- c, B;
 a, A |- b, B;
 A |- a, B.
See also CASE-REPLACE, CASE*"
 "~%Case splitting on ~@~% ~a, ~")
```

A Simple Inference Procedure: case-rule-fun

Rules return closures that are applied to a proofstate ps

A Simple Inference Procedure: case-rule-fun

The result of applying the closure is multiple values:

- A signal: '! for proved, 'X for no change, '? for new subgoals
- A list of subgoal sequents
- Side effects to the proofstate

```
(cond ((null tc-fmlas)
    (error-format-if "~%No formulas given.")
    (values 'X nil nil))
    ((not (null freevars))
    (error-format-if
    "~%Irrelevant free variables ~~a, ~ occur in formulas."
    freevars)
    (values 'X nil nil))
```

A Simple Inference Procedure

make-cases generates subgoal sequents and returns
references of tc-fmlas

The references are used to update the proofstate, when proof is completed this is used for proofchain analysis

```
(t
  (multiple-value-bind
    (subgoals dependent-decls)
    (make-cases (current-goal ps) tc-fmlas nil)
    (values '? subgoals
        (list 'dependent-decls dependent-decls))))))))
```



- Uses a BDD package written in C by Geertleon Janssen
- Uses similar addrule interface
- Uses foreign function interface for efficiency
- In addition, must translate between PVS and BDD representations

Adding a Decision Procedure: Requirements

- Decision procedures are invoked by assert, a strategy that calls the simplify primitive rule
- Decision procedures must be incremental, so they must have a state
- And they must support backtracking to an earlier state
- They must be sound
- They must be interruptible

Adding a Decision Procedure: API

- Adding a decision procedure means integrating it with simplify rule
- Instead of modifying the (very complex) simplify code, hooks have been provided
- A decision procedure is integrated by defining new methods for it



- The decision procedure language is usually first-order, and is not a subset of PVS
- Translation functions must be provided from PVS to the DP language
- If the DP is not implemented in Lisp, either interprocess communication (slow) or foreign functions must be used
- With foreign functions there is an issue with garbage collection
- Even more difficult if the DP is in a language with a garbage collector

Methods Used for Adding a Decision Procedure

- dpi-init\*: initialization invoked when PVS starts
- dpi-start\*: invoked at start of proof
- dpi-empty-state\*: used to create an empty state
- dpi-process\*: translates PVS expression, and invokes
   DP
- dpi-state-changed?\*: checks if two states are the same
- There are other optional methods available.



ICS implemented in OCaml, runtime object linked into Lisp

Defining methods was trivial

Defining foreign functions was straightforward



- OCaml garbage collector caused difficulties:
  - Externally visible pointers (data and functions) need registration
  - When a pointer is no longer needed, must be deregistered
  - Easy to forget to register something, everything seems to work
  - Difficult to debug
- OCaml also provided interrupt handlers that caused difficulties



- Immediate:
  - Write an API document
  - Theory interpretation improvements
  - Auto-forward-chaining, possibly integrated with auto-rewrite
  - XML, HTML generation
  - Improve regression test functions and add more tests
- Long Term:
  - Polymorphism
  - Add Functor sublanguage, coalgebras
  - $\circ\,$  Reflection: PVS in PVS



- Adapting existing software can be more complex than building it anew
- Though PVS was intended for embedded use, the appropriate interfaces were not adequately documented
- We are preparing a document spelling out the interfaces that are needed to integrate PVS with other software
- We are also going to contribute much of the API code to the QPQ repository (qpq.org)